## A STORY OF UNITS

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Name $\qquad$ Date $\qquad$

1. Use your folded paper strip to mark the points 0 and 1 above the number line $\frac{0}{3}, \frac{1}{3}, \frac{2}{3}, \frac{3}{3}$ below. horizontal lines to show equivalent fractions. Use multiplication to show the change in the units.


$$
\frac{1}{3}=\frac{1 \times 2}{3 \times 2}=\frac{2}{6}
$$


$\frac{1}{3}=\frac{1 \times 3}{3 \times 3}=\frac{3}{9}$

$\frac{1}{3}=\frac{1 \times 4}{3 \times 4}=\frac{4}{12}$

2. Use your folded paper strip to mark the points 0 and 1 above the number line $\frac{0}{4}, \frac{1}{4}, \frac{2}{4}, \frac{3}{4}, \frac{4}{4}$ below. Follow the same pattern as Problefm 1 but with fourths.


4. Continue the process with 9 eighths. Estimate to make the points on the number line. Do just 2

$\qquad$ Date $\qquad$

1) Show each expression on a number line. Solve.
a) $\frac{4}{9}+\frac{1}{9}$

c) $\frac{2}{7}+\frac{2}{7}+\frac{2}{7}=\frac{6}{7}$

b) $\frac{1}{4}+\frac{1}{4}+\frac{1}{4}+\frac{1}{4}=\frac{4}{4}=1$

d) $2 \times \frac{3}{5}+\frac{1}{5}=\frac{7}{5}=\frac{5}{5}+\frac{2}{5}=1 \frac{2}{5}$

2) Express each fraction as the sum of two or three equal fractional parts. Rewrite each as a multiplication equation. Show letter a on a number line.
a) $\frac{6}{11}=\frac{3}{11}+\frac{3}{11}=2 \times \frac{3}{11}$
b) $\frac{9}{4}=\frac{3}{4}+\frac{3}{4}+\frac{3}{4}=3 \times \frac{3}{4}$

c) $\frac{12}{8}=\frac{6}{8}+\frac{6}{8}=2 \times \frac{6}{8}$
d) $\frac{27}{10}=\frac{9}{10}+\frac{9}{10}+\frac{9}{10}=3 \times \frac{9}{10}$


COMMON CORE

Lesson 2:

Date:

Make equivalent fractions with sums of fractions with like denominators.
8/7/13
3) Express each of the following as the sum of a whole number and a fraction. Show c) and d) on number lines.
a) $\frac{9}{5}=\frac{5}{5}+\frac{4}{5}=1+\frac{4}{5}$
b) $\frac{7}{2}=\frac{2}{2}+\frac{2}{2}+\frac{2}{2}+\frac{1}{2}$
$=1+1+1+\frac{1}{2}$
$=3+\frac{1}{2}$
c) $\frac{25}{7}=\frac{7}{7}+\frac{7}{7}+\frac{7}{7}+\frac{4}{7}$
d) $\frac{21}{9}=\frac{9}{9}+\frac{9}{9}+\frac{3}{9}=2+\frac{3}{9}$

$$
=3+\frac{4}{7}
$$



4) Natalie sawed five boards of equal length to make a stool. Each was 9 tenths of a meter long. How many meters of board did she saw? Express your answer as the sum of a whole number and the remaining fractional units. Draw a number line to represent the problem.

$\frac{9}{10}+\frac{9}{10}+\frac{9}{10}+\frac{9}{10}+\frac{9}{10}=\frac{45}{10}$

$$
\begin{aligned}
& =\frac{10}{10}+\frac{10}{10}+\frac{10}{10}+\frac{10}{10}+\frac{5}{10} \\
& =4+\frac{5}{10}
\end{aligned}
$$



Name $\qquad$ Date $\qquad$

1. For the following problems, draw a picture using the rectangular fraction model and write the answer. Simplify your answer.
a) $\frac{1}{4}+\frac{1}{3}=\frac{3}{12}+\frac{4}{12}=\frac{7}{12}$
b) $\frac{1}{4}+\frac{1}{5}=\frac{5}{20}+\frac{4}{20}=\frac{9}{20}$

d) $\frac{1}{5}+\frac{1}{9}=\frac{9}{45}+\frac{5}{45}=\frac{14}{45}$

е) $\frac{1}{4}+\frac{2}{5}=\frac{5}{20}+\frac{8}{20}=\frac{13}{20}$
f) $\frac{3}{5}+\frac{3}{7}=\frac{21}{35}+\frac{15}{35}=\frac{36}{35}$


Solve the following problems. Draw a picture and/or write the number sentence that proves the answer.
2. Rajesh jogged $3 / 4$ mile, and then walked $1 / 6$ mile to cool down. How far did he travel?

3. Cynthia completed $2 / 3$ of the items on her to-do list in the morning, and finished $1 / 8$ of the items during her lunch break. How much of her to-do list is finished by the end of her lunch break? (Bonus: How much of her to-do list does she still have to do after lunch?)
$\frac{2}{3}+\frac{1}{8}=\frac{16}{24}+\frac{3}{24}=\frac{19}{24}$
 lunch.


## $\frac{2}{3}$

4. Sam read $2 / 5$ of her book over the weekend, and $1 / 6$ of it on Monday. What fraction of the book has she read? What fraction of the book is left?

$$
\frac{2}{5}+\frac{1}{6}=\frac{12}{30}+\frac{5}{30}=\frac{17}{30}
$$

$$
\begin{array}{r}
30 \\
-17 \\
\hline 13
\end{array}
$$



Sam read $\frac{17}{30}$ of the book. He still has $\frac{13}{30}$ of the book left over.

Name $\qquad$ Date $\qquad$

1. Directions: For the following problems, draw a picture using the rectangular fraction model and write the answer. When possible, write your answer as a mixed number.

c) $\frac{1}{3}+\frac{3}{5}=\frac{5}{15}+\frac{9}{15}=\frac{14}{15}$

d) $\frac{5}{6}+\frac{1}{2}=\frac{10}{12}+\frac{6}{12}=\frac{16}{12}=1 \frac{4}{12}$ or $1 \frac{1}{3}$

$\frac{12}{12} \quad \frac{4}{12}$
e) $\frac{2}{3}+\frac{5}{6}=\frac{12}{18}+\frac{15}{18}=\frac{27}{18}=1 \frac{9}{18}$
f) $\frac{4}{3}+\frac{4}{7}=\frac{28}{21}+\frac{12}{21}=\frac{40}{21}=\frac{21}{21}+\frac{19}{21}=1 \frac{19}{21}$


Solve the following problems. Draw a picture and/or write the number sentence that proves the answer. Simplify your answer.
2. Sam made $2 / 3$ liter of punch and $3 / 4$ liter of tea to take to a party. How many liters of beverages did Sam bring to the party?

$$
\frac{2}{3}+\frac{3}{4}=\frac{8}{12}+\frac{9}{12}=\frac{17}{12}=\frac{12}{12}+\frac{5}{12}=1 \frac{5}{12}
$$

|  |  |  |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |
|  |  |  |


|  |  |  |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |
|  |  |  |

Sam brought $1 \frac{5}{12}$ liters of beverages to the party.
3) Mr. Sinofsky used $5 / 8$ of a tank of gas on a trip to visit relatives for the weekend and another half of a tank commuting to work the next week. He then took another weekend trip and used $1 / 4$ tank of gas. How many tanks of gas did Mr. Sinofsky use altogether?

$$
\begin{aligned}
& \frac{1}{2}+\frac{1}{4}=\frac{3}{4} \\
& \frac{5}{8}+\frac{3}{4}=\frac{20}{32}+\frac{24}{32}=\frac{44}{32}=\frac{32}{32}+\frac{12}{32}=1 \frac{12}{32} \\
& 1 \frac{12}{32}=1 \frac{6}{16}=1 \frac{3}{8}
\end{aligned}
$$

Mr. Sinofsky used $1 \frac{3}{8}$ tanks of gas.

Name $\qquad$ Date $\qquad$

1. The picture below shows $\frac{3}{4}$ of the rectangle shaded. Use the picture to show how to create an equivalent fraction for $\frac{3}{4}$, and then subtract $\frac{1}{3}$.


$$
\frac{3}{4}-\frac{1}{3}=\frac{9}{12}-\frac{4}{12}=\frac{5}{12}
$$


2. Find the difference. Use a rectangular fraction model to find common denominators. Simplify your answer, if possible.
a. $\frac{5}{6}-\frac{1}{3}=\frac{15}{18}-\frac{6}{18}=\frac{9}{18}=\frac{1}{2}$
b. $\frac{2}{3}-\frac{1}{2}=\frac{4}{6}-\frac{3}{6}=\frac{1}{6}$

c. $\frac{5}{6}-\frac{1}{4}=\frac{20}{24}-\frac{6}{24}=\frac{14}{24}=\frac{7}{12}$
d. $\frac{4}{5}-\frac{1}{2}=\frac{8}{10}-\frac{5}{10}=\frac{3}{10}$

e. ${ }_{3}^{2}-\frac{2}{5}=\frac{10}{15}-\frac{6}{15}=\frac{4}{15}$
f. $\frac{5}{7}-\frac{2}{3}=\frac{15}{21}-\frac{14}{21}=\frac{1}{21}$

3. Robin used $\frac{1}{4}$ of a pound of butter to make a cake. Before she started, she had $\frac{7}{8}$ of a pound of butter. How much butter did Robin have when she was done baking? Give your answer as a fraction of a pound.

$$
\frac{7}{8}-\frac{1}{4}=\frac{28}{32}-\frac{8}{32}=\frac{20}{32}=\frac{10}{16}=\frac{5}{8}
$$

## Robin had $\frac{5}{8}$ of a pound of butter left aver.

4. Katrina needs $\frac{3}{5}$ kilogram of flour for a recipe. Her mother has $\frac{3}{7}$ kilogram of flour in her pantry. Is this enough flour for the recipe? If not, how much more will she need?

We know $\frac{3}{5}$ is larger than $\frac{3}{7}$ because tape diagrams "prove" it.

$\frac{3}{7}$


$$
\frac{3}{5}-\frac{3}{7}=\frac{21}{35}-\frac{15}{35}=\frac{6}{35}
$$

NOTE: Since the re are a variety of methods to solve these problems, we

Name will demonstrate that variety in the answer key. Date $\qquad$

1. Find the difference. Use a rectangular fraction model to show how to convert to fractions with common denominators.
a) $1-\frac{5}{6}=\frac{6}{6}-\frac{5}{6}=\frac{1}{6}$

c) $\frac{4}{3}-\frac{5}{7}=\frac{28}{21}-\frac{15}{21}=\frac{13}{21}$
d) $1 \frac{1}{8}-\frac{3}{5}=$

f) $1 \frac{5}{6}-\frac{7}{8}=\frac{88}{48}-\frac{56}{48}=\frac{32}{48}=\frac{4}{6}=\frac{2}{3}$

g) $1 \frac{2}{7}-\frac{3}{4}=\frac{1}{4}+\frac{2}{7}$
$\frac{4^{2}}{4} \frac{2}{7}=\frac{7}{28}+\frac{8}{28}=\frac{15}{28}$
h) $1 \frac{3}{12}-\frac{2}{3}=\frac{12}{36}+\frac{9}{36}=\frac{21}{36}=\frac{7}{12}$

$$
\begin{array}{lll}
\frac{36}{36} & \frac{9}{36} & \frac{34}{36}
\end{array}
$$



COMMON CORE

Lesson 6: Date:

Subtract fractions from numbers between 1 and 2 . 8/7/13
2. Sam had $11 / 2 \mathrm{~m}$ of rope. He cut off $5 / 8 \mathrm{~m}$ and used it for a project. How much rope does Sam have left?

$1 \frac{1}{2}-\frac{5}{8}=\frac{24}{16}-\frac{10}{16}=\frac{14}{16}=\frac{7}{8}$
Sam has $\frac{7}{8} m$ left over.
3. Jackson had $13 / 8 \mathrm{~kg}$ of fertilizer. He used some to fertilize a flower bed andre only had $2 / 3 \mathrm{~kg}$ left. How much fertilizer was used in the flower bed


$$
\begin{aligned}
& 1 \frac{3}{8}-\frac{2}{3}=\frac{8}{24}+\frac{9}{24}=\frac{17}{24} \\
& \frac{24}{24}+\frac{9}{24}-\frac{16}{24} \\
& \text { Jackson used } \frac{17}{24} \mathrm{~kg} \text { of fertilizer } \\
& \text { in the flower bed. }
\end{aligned}
$$

Name $\qquad$ Date $\qquad$

Solve the word problem using the RDW strategy. Show all your work.

1. Christine baked a pumpkin pie. She ate $1 / 6$ of the pie. Her brother ate $1 / 3$ of it, and gave the left overs to his friends. What fraction of the pie did he give to his friends?

$$
\frac{1}{6}+\frac{1}{3}=\frac{3}{18}+\frac{6}{18}=\frac{9}{18}=\frac{1}{2}
$$

$$
1-\frac{1}{2}=\frac{1}{2}
$$

 He gave $\frac{1}{2}$ of the pie to his friends.
2. Liang went to the bookstore. He spent $1 / 3$ of his money on a pen and $4 / 7$ of it on books. What fraction of his money did he have left?


$$
\begin{aligned}
& \frac{1}{3}+\frac{4}{7}=\frac{7}{21}+\frac{12}{21}=\frac{19}{21} \\
& 1-\frac{19}{21}=\frac{21}{21}-\frac{19}{21}=\frac{2}{21}
\end{aligned}
$$

Lang has $\frac{2}{\partial 1}$ of his money left over.
3. Tiffany bought $2 / 5 \mathrm{~kg}$ of cherries. Linda bought $1 / 10 \mathrm{~kg}$ of cherries less than Tiffany. How many kg of cherries did they buy altogether?


$$
\frac{2}{5}-\frac{1}{10}=\frac{4}{10}-\frac{1}{10}=\frac{3}{10}
$$

Linda bought $\frac{3}{10} \mathrm{~kg}$ of cherries.

$$
\frac{2}{5}+\frac{3}{10}=\frac{4}{10}+\frac{3}{10}=\frac{7}{10}
$$

Altogether, they bought $\frac{7}{10} \mathrm{~kg}$ of cherries.
4. Mr. Rivas bought a can of paint. He used $3 / 8$ of it to paint a book shelf. He used $1 / 4$ of it to paint a wagon. He used some of it to paint a bird house, and have $1 / 8$ of paint left. How much paint did he use for the bird house?


$$
\begin{aligned}
& \frac{3}{8}+\frac{1}{8}+\frac{1}{4}=\frac{4}{8}+\frac{1}{4}=\frac{3}{4} \\
& 1-\frac{3}{4}=\frac{4}{4}-\frac{3}{4}=\frac{1}{4}
\end{aligned}
$$

Mr. Rivas used $\frac{1}{4}$ of the paint for the bird house.
5. Ribbon $A$ is $1 / 3 \mathrm{~m}$ long. It is $2 / 5 \mathrm{~m}$ shorter than ribbon $B$. What's the total length of two ribbons?



$$
\begin{aligned}
\frac{1}{3}+\frac{1}{3}+\frac{2}{5} & =\frac{2}{3}+\frac{2}{5} \\
& =\frac{10}{15}+\frac{6}{15} \\
& =\frac{16}{15} \\
& =1 \frac{1}{15}
\end{aligned}
$$

The total length of the two ribbons is $1 \frac{1}{15}$ meters.

Name $\qquad$ Date $\qquad$

1. Add or subtract.

e) $8 \frac{4}{5}+7=15 \frac{4}{5}$

g) $16+18 \frac{5}{6}=34 \frac{5}{6}$

f) $18-15 \frac{3}{4}=2 \frac{1}{4}$

h) $100-50 \frac{3}{8}=49 \frac{5}{8}$

2. The total length of two ribbons is 13 meters. If one ribbon is $7 \frac{5}{8}$ meters long, what is the length of the other ribbon?

3. It took Sandy two hours to jog 13 miles. She ran $71 / 2$ miles in the first hour. How far did she run during the second hour?


$$
\begin{aligned}
13-7 \frac{1}{2} & =13-7-\frac{1}{2} \\
& =6-\frac{1}{2} \\
& =5 \frac{1}{2}
\end{aligned}
$$


4. Andre says that $5 \frac{3}{4}+2 \frac{1}{4}=7 \frac{1}{2}$ because $7 \frac{4}{8}=7 \frac{1}{2}$. Identify his mistake. Draw a picture to prove that he is wrong.
Andre is wrong because he added the denominators when he should only add the numerators.


$$
5 \frac{3}{4}+2 \frac{1}{4}=8
$$

 equivalence and the number line as strategies.
Date: 8/7/13
$\qquad$
$\qquad$

1. Make like units, then add. Use an equation to show your thinking.
a) $\frac{3}{5}+\frac{1}{3}=\left(\frac{3}{5} \times \frac{3}{3}\right)+\left(\frac{1}{3} \times \frac{5}{5}\right)$

$$
=\frac{9}{15}+\frac{5}{15}
$$

$$
=\frac{14}{15}
$$

$$
\text { b) } \begin{aligned}
\frac{3}{5}+\frac{1}{11} & =\left(\frac{3}{5} \times \frac{11}{11}\right)+\left(\frac{1}{11} \times \frac{5}{5}\right) \\
& =\frac{33}{55}+\frac{5}{55} \\
& =\frac{38}{55}
\end{aligned}
$$

c) $\frac{2}{9}+\frac{5}{6}=\left(\frac{2}{9} \times \frac{2}{2}\right)+\left(\frac{5}{6} \times \frac{3}{3}\right)$
d) $\frac{2}{5}+\frac{1}{4}+\frac{1}{10}=\left(\frac{2}{5} \times \frac{4}{4}\right)+\left(\frac{1}{4} \times \frac{5}{5}\right)+\left(\frac{1}{10} \times \frac{2}{2}\right)$

$$
=\frac{4}{18}+\frac{15}{18}
$$

$$
=\frac{8}{20}+\frac{5}{20}+\frac{2}{20}
$$

$$
=\frac{19}{18}=1 \frac{1}{18}
$$

е) $\frac{1}{3}+\frac{7}{5}=\left(\frac{1}{3} \times \frac{5}{5}\right)+\left(\frac{7}{5} \times \frac{3}{3}\right)$
f) $\frac{5}{8}+\frac{7}{12}=\left(\frac{5}{8} \times \frac{3}{3}\right)+\left(\frac{7}{12} \times \frac{2}{2}\right)$

$$
\begin{aligned}
& =\frac{5}{15}+\frac{21}{15} \\
& =\frac{26}{15}=1 \frac{11}{15}
\end{aligned}
$$

g) $1 \frac{1}{3}+\frac{3}{4}=1+\left(\frac{1}{3} \times \frac{4}{4}\right)+\left(\frac{3}{4} \times \frac{3}{3}\right)$

$$
=1+\frac{4}{12}+\frac{9}{12}
$$

$=1+\frac{13}{12}$

$$
=1+1 \frac{1}{\sqrt{2}}=2 \frac{1}{12}
$$

h) $\frac{5}{6}+1 \frac{1}{4}=\left(\frac{5}{6} \times \frac{2}{2}\right)+1+\left(\frac{1}{4} \times \frac{3}{3}\right)$

$$
=\frac{10}{12}+1+\frac{3}{12}
$$

$$
=1+\frac{13}{12}
$$

$$
=1 \pm 1 \frac{1}{12}=2 \frac{1}{12}
$$

2. On Monday, Ka practices guitar for $\frac{2}{3}$ of one hour. When she's finished, she practices piano for $\frac{3}{4}$ of one hour. How much time did Ka spend practicing instruments on Monday?


$$
\begin{aligned}
\frac{2}{3}+\frac{3}{4} & =\left(\frac{2}{3} \times \frac{4}{4}\right)+\left(\frac{3}{4} \times \frac{3}{3}\right) \\
& =\frac{8}{12}+\frac{9}{12} \\
& =\frac{17}{12} \\
& =1 \frac{5}{12}
\end{aligned}
$$

3. Ms. How buys a bag of rice to cook dinner. She used $\frac{3}{5} \mathrm{~kg}$ of rice and still had $2 \frac{1}{4} \mathrm{~kg}$ left. How heavy was the bag of rice that Ms. How bought?


$$
\begin{aligned}
2 \frac{1}{4}+\frac{3}{5} & =2+\frac{1}{4}+\frac{3}{5} \\
& =2+\left(\frac{1}{4} \times \frac{5}{5}\right)+\left(\frac{3}{5} \times \frac{4}{4}\right) \\
& =2+\frac{5}{20}+\frac{12}{20} \\
& =2 \frac{17}{20}
\end{aligned}
$$

4. Joe spends $\frac{2}{5}$ of his money on a jacket and $\frac{3}{8}$ of his money on a shirt. He spends the rest on a pair of pants. What fraction of his money does he use to buy the pants?

$$
\begin{aligned}
\frac{2}{5}+\frac{3}{8} & =\left(\frac{2}{5} \times \frac{8}{8}\right)+\left(\frac{3}{8} \times \frac{5}{5}\right) \\
& =\frac{16}{40}+\frac{15}{40} \\
& =\frac{31}{40} \\
1-\frac{31}{40} & =\frac{40}{40}-\frac{31}{40}=\frac{9}{40}
\end{aligned}
$$

Joe spent $\frac{9}{40}$ of his money on pants.

Name $\qquad$ Date $\qquad$

1. Add.
a) $2 \frac{1}{2}+1 \frac{1}{5}=3+\frac{1}{2}+\frac{1}{5}$
b) $2 \frac{1}{2}+1 \frac{3}{5}=3+\frac{1}{2}+\frac{3}{5}$

$$
=3+\left(\frac{1}{2} \times \frac{5}{5}\right)+\left(\frac{1}{5} \times \frac{2}{2}\right)
$$ $=3+\left(\frac{1}{2} \times \frac{5}{5}\right)+\left(\frac{3}{5} \times \frac{2}{2}\right)$

$$
=3+\frac{5}{10}+\frac{2}{10}
$$

$=3+\frac{5}{10}+\frac{6}{10}$

$$
=3 \frac{7}{10}
$$

$$
=3+\frac{11}{10}=3+1 \frac{1}{10}=4 \frac{1}{10}
$$

c) $1 \frac{1}{5}+3 \frac{1}{3}=4+\frac{1}{5}+\frac{1}{3}$

$$
\begin{aligned}
& =4+\left(\frac{1}{5} \times \frac{3}{3}\right)+\left(\frac{1}{3}+\frac{5}{5}\right) \\
& =4+\frac{3}{15}+\frac{5}{15} \\
& =4 \frac{8}{15}
\end{aligned}
$$

e) $2 \frac{1}{3}+4 \frac{4}{7}=6+\frac{1}{3}+\frac{4}{7}$

$$
\begin{aligned}
& =6+\left(\frac{1}{3} \times \frac{7}{7}\right)+\left(\frac{4}{7} \times \frac{3}{3}\right) \\
& =6+\frac{7}{21}+\frac{12}{21} \\
& =6 \frac{19}{21}
\end{aligned}
$$

g) $15 \frac{1}{5}+4 \frac{3}{8}=19+\frac{1}{5}+\frac{3}{8}$

$$
\begin{aligned}
& =19+\left(\frac{5}{5} \times \frac{8}{8}\right)+\left(\frac{3}{8} \times \frac{5}{5}\right) \\
& =19+\frac{8}{40}+\frac{15}{40} \\
& =19+\frac{23}{40} \\
& =12 \frac{23}{40}
\end{aligned}
$$

d) $3 \frac{2}{3}+1 \frac{3}{5}=4+\frac{2}{3}+\frac{3}{5}$
$=4+\left(\frac{2}{3} \times \frac{5}{5}\right)+\left(\frac{3}{5} \times \frac{3}{3}\right)$
$=4+\frac{10}{15}+\frac{9}{15}$
$=4+\frac{19}{15}=5 \frac{4}{15}$
f) $3 \frac{5}{7}+4 \frac{2}{3}=7+\frac{5}{7}+\frac{2}{3}$

$$
\begin{aligned}
& =7+\left(\frac{5}{7} \times \frac{3}{3}\right)+\left(\frac{2}{3} \times \frac{7}{7}\right) \\
& =7+\frac{15}{21}+\frac{14}{21} \\
& =7+\frac{29}{21}=8 \frac{8}{21}
\end{aligned}
$$

h) $18 \frac{3}{8}+2 \frac{2}{5}=20+\frac{3}{8}+\frac{2}{5}$

$$
\begin{aligned}
& =20+\left(\frac{3}{8} \times \frac{5}{5}\right)+\left(\frac{2}{5} \times \frac{8}{8}\right) \\
& =20+\frac{15}{40}+\frac{16}{40} \\
& =20+\frac{31}{40} \\
& =20 \frac{31}{40}
\end{aligned}
$$

2. Angela practiced piano for $2 \frac{1}{2}$ hours on Friday, $2 \frac{1}{3}$ hours on Saturday, and $3 \frac{2}{3}$ hours on Sunday. How much time did Angela practice piano during the weekend?

$$
\begin{aligned}
2 \frac{1}{2}+2 \frac{1}{3}+3 \frac{2}{3} & =7+\frac{1}{2}+\frac{1}{3}+\frac{2}{3} \\
& =8 \frac{1}{2}
\end{aligned}
$$

Angela practiced $8 \frac{1}{2}$ hours during the weekend.
3. String $A$ is $3 \frac{5}{6}$ meters long. String $B$ is $2 \frac{1}{4}$ long. What's the total length of both strings?


$$
\begin{aligned}
3 \frac{5}{6}+2 \frac{1}{4} & =5+\frac{5}{6}+\frac{1}{4} \\
& =5+\left(\frac{5}{6} \times \frac{2}{2}\right)+\left(\frac{1}{4} \times \frac{3}{3}\right) \\
& =5+\frac{10}{12}+\frac{3}{12} \\
& =5+\frac{13}{12} \quad \text { The total length of } \\
& =6 \frac{1}{12} \quad \text { both string is }
\end{aligned}
$$

4. Matt says that $5-1 \frac{1}{4}$ will be more than 4 , since $5-1$ is 4 . Draw a picture to prove that Matt is wrong.


Matt is wrong because the picture shows the answer should be $3 \frac{3}{4}$.
$\qquad$ Date $\qquad$

1. First find a common unit, then subtract.
a. $\frac{1}{2}-\frac{1}{5}=\left(\frac{1}{2} \times \frac{5}{5}\right)-\left(\frac{1}{5} \times \frac{2}{2}\right)$

$$
=\frac{5}{10}-\frac{2}{10}
$$

$$
=\frac{3}{10}
$$

$$
\text { b. } \begin{aligned}
\frac{7}{8}-\frac{1}{3} & =\left(\frac{7}{8} \times \frac{3}{3}\right)-\left(\frac{1}{3} \times \frac{8}{8}\right) \\
& =\frac{21}{24}-\frac{8}{24} \\
& =\frac{13}{24}
\end{aligned}
$$

c. $\frac{7}{10}-\frac{3}{5}=\frac{7}{10}-\left(\frac{3}{5} \times \frac{2}{2}\right)$
d. $1 \frac{5}{6}-\frac{2}{3}=1+\frac{5}{6}-\frac{2}{3}$

$$
\begin{aligned}
& =\frac{7}{10}-\frac{6}{10} \\
& =\frac{1}{10}
\end{aligned}
$$

e. $2 \frac{1}{4}-1 \frac{1}{5}=1 \frac{1}{4}-\frac{1}{5}$
f. $5 \frac{6}{7}-3 \frac{2}{3}=2 \frac{6}{7}-\frac{2}{3}$

$$
\begin{aligned}
& =1+\left(\frac{1}{4} \times \frac{5}{5}\right)-\left(\frac{1}{5} \times \frac{4}{4}\right) \\
& =1+\frac{5}{20}-\frac{4}{20} \\
& =1 \frac{1}{20}
\end{aligned}
$$

g. $15 \frac{7}{8}-5 \frac{3}{4}=10 \frac{7}{8}-\frac{3}{4}$

$$
\begin{aligned}
& =10+\frac{7}{8}-\left(\frac{3}{4} \times \frac{2}{2}\right) \\
& =10+\frac{7}{8}-\frac{6}{8} \\
& =10 \frac{1}{8}
\end{aligned}
$$

h. $15 \frac{5}{8}-3 \frac{1}{3}=12 \frac{5}{8}-\frac{1}{3}$

$$
\begin{aligned}
& =12+\left(\frac{5}{8} \times \frac{3}{3}\right)-\left(\frac{1}{3} \times \frac{8}{8}\right) \\
& =12+\frac{15}{24}-\frac{8}{24} \\
& =12 \frac{7}{24}
\end{aligned}
$$

2. Sandy ate $\frac{1}{6}$ of a candy bar. John ate $\frac{3}{4}$ of it. How much more of the candy bar did John eat than Sandy? $\frac{3}{4}-\frac{1}{6}=\left(\frac{3}{4} \times \frac{3}{3}\right)-\left(\frac{1}{6} \times \frac{2}{2}\right)$ John ate $\frac{7}{12}$ of the candy bar more than Sandy.
3. $4 \frac{1}{2}$ yards of cloth are needed to make a woman's dress. $2 \frac{2}{7}$ yards of cloth are needed to make a girl's dress. How much more cloth is needed to make a woman's dress than a girl's dress?

$$
\begin{aligned}
4 \frac{1}{2}-2 \frac{2}{7} & =2 \frac{1}{2}-\frac{2}{7} & & \text { To make a woman's dress, } 2 \frac{3}{14} \text { yards } \\
& =2+\left(\frac{1}{2} \times \frac{7}{7}\right)-\left(\frac{2}{7} \times \frac{2}{2}\right) & & \text { more cloth is needed than a girl's dress. } \\
& =2+\frac{7}{14}-\frac{4}{14} & &
\end{aligned}
$$

4. Bill reads $\frac{1}{5}$ of a book on Monday. He reads $\frac{2}{3}$ of the book on Tuesday. If he finishes reading the book on Wednesday, what fraction of the book did he read on Wednesday?


$$
\begin{aligned}
\frac{1}{5}+\frac{2}{3} & =\left(\frac{1}{5} \times \frac{3}{3}\right)+\left(\frac{2}{3} \times \frac{5}{5}\right) \\
& =\frac{3}{15}+\frac{10}{15} \\
& =\frac{13}{15} \\
1 & -\frac{13}{15}=\frac{2}{15}
\end{aligned}
$$

5. Tank A has a capacity of 9.5 gallons. $6 \frac{1}{3}$ gallons of the tank's water are poured out. How much water is left in the tank?

$$
\begin{aligned}
& 9.5-6 \frac{1}{3} \\
& 9 \frac{1}{2}-6 \frac{1}{3}=3 \frac{1}{2}-\frac{1}{3} \\
&=3+\left(\frac{1}{2} \times \frac{3}{3}\right)-\left(\frac{1}{3} \times \frac{2}{2}\right) \\
&=3+\frac{3}{6}-\frac{2}{6} \\
&=3 \frac{1}{6}
\end{aligned}
$$

$\qquad$ Date $\qquad$

1. Subtract.

$$
\begin{aligned}
& \text { a) } 3 \frac{1}{4}-2 \frac{1}{3}= \\
&= 1 \frac{1}{4}-\frac{1}{3} \\
&= \frac{12}{12}+\frac{3}{12}-\frac{4}{12}=\frac{11}{12}
\end{aligned}
$$

c) $6 \frac{1}{5}-4 \frac{1}{4}=$

$$
\begin{aligned}
& =2 \frac{1}{5}-\frac{1}{4} \\
& =1+\frac{3}{4}+\frac{1}{5}=1+\frac{15}{20}+\frac{4}{20}=1 \frac{19}{20}
\end{aligned}
$$

e) $5 \frac{2}{7}-4 \frac{1}{3}=$

$$
=\begin{aligned}
= & \frac{2}{7}-\frac{1}{3} \\
& \frac{3}{3}+\frac{2}{7}-\frac{1}{3}=\frac{2}{3}+\frac{2}{7}=\frac{14}{21}+\frac{6}{21}=\frac{20}{21}
\end{aligned}
$$

g) $18 \frac{3}{4}-5 \frac{7}{8}=$

$$
\begin{aligned}
& =13 \frac{3}{4}-\frac{7}{8} \\
& =12 \frac{7}{4}-\frac{7}{8}=12 \frac{14}{8}-\frac{7}{8}=12 \frac{7}{8}
\end{aligned}
$$

b) $3 \frac{2}{3}-2 \frac{3}{4}=$

$$
\begin{aligned}
& =1 \frac{2}{3}-\frac{3}{4} \\
& =\frac{12}{12}+\frac{8}{12}-\frac{9}{12}=\frac{11}{12}
\end{aligned}
$$

d) $6 \frac{3}{5}-4 \frac{3}{4}=$

$$
\begin{aligned}
& =2 \frac{3}{5}-\frac{3}{4} \\
& =1 \frac{8}{5}-\frac{3}{4}=1 \frac{32}{20}-\frac{15}{20}=1 \frac{17}{20}
\end{aligned}
$$

f) $8 \frac{2}{3}-3 \frac{5}{7}=$

$$
=5 \frac{2}{3}-\frac{5}{7}
$$

$$
=4 \frac{5}{3}-\frac{5}{7}=4 \frac{35}{21}-\frac{15}{21}=4 \frac{20}{21}
$$

h) $17 \frac{1}{5}-2 \frac{5}{8}=$

$$
=15 \frac{1}{5}-\frac{5}{8}
$$

$$
=14 \frac{6}{5}-\frac{5}{8}=14 \frac{48}{40}-\frac{25}{40}=14 \frac{23}{40}
$$

2. Tony wrote the following:

$$
7 \frac{1}{4}-3 \frac{3}{4}=4 \frac{1}{4}-\frac{3}{4}
$$

Is Tony's statement correct? Draw a diagram to support your answer.


Tony is correct because the drawing shows that we are allowed to subtract the whole numbers before subtracting $3 / 4$.
3. Ms. Sanger blended $8 \frac{3}{4}$ gallons of iced tea with some lemonade for a picnic. If there were $13 \frac{2}{5}$ gallons in the mixture, how many gallons of lemonade did she use?


$4+\frac{5}{20}+\frac{8}{20}$


She used $4 \frac{13}{20}$ gallons of lemonade.
4. A carpenter has a $10 \frac{1}{2}$ foot wood plank. He cuts off $4 \frac{1}{4}$ feet to replace the slat of a deck and $3 \frac{2}{3}$ feet to repair a bannister. He uses the rest of the plank to fix a stair. How many feet of wood does the carpenter use to fix the stair?

$$
\begin{aligned}
4 \frac{1}{4}+3 \frac{2}{3} & =7 \frac{1}{4}+\frac{2}{3}=7 \frac{3}{12}+\frac{8}{12}=7 \frac{11}{12} \\
10 \frac{1}{2}-7 \frac{11}{12} & =3 \frac{1}{2}-\frac{11}{12} \\
& =2+\frac{12}{12}+\frac{6}{12}-\frac{11}{12} \\
& =2 \frac{7}{12}
\end{aligned}
$$

The carpenter has $2 \frac{7}{12}$ feet of wood to fix the stairs.

Name $\qquad$ Date $\qquad$

1. Are the following greater than or less than 1 ? Circle the correct answer.
a) $\frac{1}{2}+\frac{4}{9}$
greater than 1

b) $\frac{5}{8}+\frac{3}{5}$


$$
\text { less than } 1
$$

c) $1 \frac{1}{5}-\frac{1}{3}$
greater than 1

d) $4 \frac{3}{5}-3 \frac{3}{4}$
greater than 1

2. Are the following greater than or less than $1 / 2$ ? Circle the correct answer.
e) $\frac{1}{5}+\frac{1}{4}$
greater than $\frac{1}{2}$
less than $\frac{1}{2}$
f) $\frac{6}{7}-\frac{1}{6}$

less than $\frac{1}{2}$
g) $1 \frac{1}{7}-\frac{5}{6}$
greater than $\frac{1}{2}$

h) $\frac{4}{7}+\frac{1}{8}$

less than $\frac{1}{2}$
3. Use $>,<$, or $=$ to make the following statements true.
i) $5 \frac{4}{5}+2 \frac{2}{3} \leq 8 \frac{3}{4}$
j) $3 \frac{4}{7}-2 \frac{3}{5}<1 \frac{4}{7}+\frac{3}{5}$
k) $4 \frac{1}{2}+1 \frac{4}{9}>5+\frac{13}{18}$
I) $10 \frac{3}{8}-7 \frac{3}{5}<3 \frac{3}{8}+\frac{3}{5}$

NOT EQUAL
4. Is it true that $5 \frac{2}{3}-3 \frac{3}{4}=1+\frac{2}{3}+\frac{3}{4}$ ? Prove your answer.

$$
\begin{aligned}
& 5 \frac{2}{3}-3 \frac{3}{4} \\
& \begin{aligned}
2 \frac{2}{3}-\frac{3}{4} & =1+1+\frac{2}{3}-\frac{3}{4} \\
& =1+\frac{4}{4}+\frac{2}{3}-\frac{3}{4} \\
& =1+\frac{2}{3}+\frac{1}{4}
\end{aligned}
\end{aligned}
$$

5. A tree limb hangs $5 \frac{1}{4}$ feet from a telephone wire. The city trims back the branch before it grows within $2 \frac{1}{2}$ feet of the wire. Will the city allow the tree to grow $2 \frac{3}{4}$ more feet?

$$
\begin{aligned}
5 \frac{1}{4}-2 \frac{3}{4} & =4+\frac{4}{4}+\frac{1}{4}-2-\frac{3}{4} \\
& =2+\frac{1}{4}+\frac{1}{4}=2 \frac{1}{2}
\end{aligned}
$$

Once the tree grows $2 \frac{3}{4}$ feet it will be exactly $2 \frac{1}{2}$ feet from the wire, so the city would trim it.
6. Mr. Kreider wants to paint two doors and several shutters. It takes $2 \frac{1}{8}$ gallons of paint to coat each door and $1 \frac{3}{5}$ gallons of paint to coat his shutters. If Mr. Kreider buys three 2-gallon cans of paint, does he have enough to complete the job?

$$
2 \frac{1}{8}+2 \frac{1}{8}+1 \frac{3}{5}=4 \frac{2}{8}+1 \frac{3}{5}=5 \frac{2}{8}+\frac{3}{5}=5 \frac{10}{40}+\frac{24}{40}=5 \frac{34}{40}
$$

$$
5 \frac{34}{40}<6
$$

Mr.KReider has enough paint to complete the job. addition and subtraction equations.
Date:
$\qquad$ Date $\qquad$

1. Rearrange the terms so that you can add or subtract mentally, then solve.
a) $1 \frac{3}{4}+\frac{1}{2}+\frac{1}{4}+\frac{1}{2}$
$2+1=3$
b) $3 \frac{1}{6}-\frac{3}{4}+\frac{5}{6}$
d) $\frac{\frac{7}{9}+\frac{1}{2}-\frac{3}{2}+\frac{2}{9}}{\frac{3}{2}-\frac{1}{2}-\frac{3}{2}}=0$
2. Fill in the blank to make the statement true.

$$
\text { g) } \begin{aligned}
& 7 \frac{3}{4}-1 \frac{2}{7}-\frac{3}{2}=4 \frac{27}{28} \\
& 7 \frac{21}{28}-1 \frac{8}{28}-1 \frac{1}{2} \\
& 6 \frac{13}{28}-1 \frac{1}{2} \\
& 5 \frac{13}{28}-\frac{1}{2}=4 \frac{41}{28}-\frac{14}{28}=4 \frac{27}{28}
\end{aligned}
$$

h) $9 \frac{5}{6}+1 \frac{1}{4}+\sum \frac{11}{12}=14$

$$
10 \frac{5}{6}+\frac{1}{4}
$$

$$
10 \frac{10}{12}+\frac{3}{12}=10 \frac{13}{12}=11 \frac{1}{12}
$$

$$
\text { i) } \frac{7}{10}-\sqrt{4}+\frac{3}{2}=\frac{6}{5}
$$

ј) $37 \frac{7}{8}-20-3 \frac{1}{4}=14 \frac{5}{8} \quad 23 \frac{1}{4}+14 \frac{5}{8}$

$$
\frac{7}{10}-\square+\frac{15}{10}=\frac{12}{10}
$$

$\square-23 \frac{1}{4}=14 \frac{5}{8}$

$$
\frac{22}{10}-\frac{10}{10}=\frac{12}{10}
$$

$$
\begin{gathered}
23 \frac{2}{8}+14 \frac{5}{8} \\
37 \frac{7}{8}
\end{gathered}
$$

$10 \frac{4}{5}-8 \frac{1}{6}$
k) $\frac{17}{3}+2 \frac{19}{30}+\frac{5}{2}=10 \frac{4}{5}$
$10 \frac{24}{30}-8 \frac{5}{30}$

$$
5 \frac{2}{3}+-2 \frac{1}{2}
$$


3. Laura bought $8 \frac{3}{10}$ yd of ribbon. She used $1 \frac{2}{5}$ yd to tie a package and $2 \frac{1}{3}$ to make a bow. Joe later gave her $4 \frac{3}{5}$ yd. How much ribbon does she now have?

$$
8 \frac{3}{10}+4 \frac{3}{5}-1 \frac{2}{5}-2 \frac{1}{3}
$$

$$
\underbrace{8 \frac{3}{10}+4 \frac{6}{10}-1 \frac{4}{10}-2 \frac{1}{3}}_{11 \frac{5}{10}-2 \frac{1}{3}}
$$

$$
11 \frac{1}{2}-2 \frac{1}{3}
$$

$$
11 \frac{3}{6}-2 \frac{2}{6}=9 \frac{1}{6}
$$

4. Mia bought $10 \frac{1}{9} \mathrm{lb}$ of flour. She used $2 \frac{3}{4} \mathrm{lb}$ of flour to bake a banana cake and some to bake a chocolate cake. After baking the two cakes, she had $3 \frac{5}{6} \mathrm{lb}$ of flour left. How much flour did she use to bake the chocolate cake?


$$
\begin{aligned}
2 \frac{3}{4}+3 \frac{5}{6} & =5 \frac{3}{4}+\frac{5}{6} \\
& =5 \frac{9}{12}+\frac{10}{12} \\
& =5 \frac{19}{12}=6 \frac{1}{12}
\end{aligned}
$$

$$
\begin{aligned}
& 10 \frac{1}{9}-6 \frac{7}{12} \\
& 4 \frac{1}{9}-\frac{7}{12} \\
& 4 \frac{4}{36}-\frac{21}{36} \\
& 3 \frac{40}{36}-\frac{21}{36}=3 \frac{19}{36}
\end{aligned}
$$

$\qquad$ Date $\qquad$

Solve the word problems using the RDW strategy. Show all your work.

1. A baker buys a 5 lb bag of sugar. She uses $1 \frac{2}{3} \mathrm{lb}$ to make some muffins and $2 \frac{3}{4} \mathrm{lb}$ to make a cake. How much sugar does she have left?


$$
\begin{aligned}
& 1 \frac{2}{3}+2 \frac{3}{4}=3 \frac{2}{3}+\frac{3}{4}=3+\frac{8}{12}+\frac{9}{12}=3 \frac{17}{12}=4 \frac{5}{12} \\
& 5-4 \frac{5}{12}=1-\frac{5}{12}=\frac{12}{12}-\frac{5}{12}=\frac{7}{12}
\end{aligned}
$$

The baker has $\frac{7}{12}$ pound of sugar left over.
2. A boxer needs to lose $3 \frac{1}{2} \mathrm{~kg}$ in a month to be able to compete as a flyweight. In three weeks, he lowers his weight from 55.5 kg to 53.8 kg . How many kg must the boxer lose in the final week to be able to compete as a flyweight?

$$
\begin{gathered}
55 \frac{5}{10}-53 \frac{8}{10}=2 \frac{5}{10}-\frac{8}{10}=1 \frac{15}{10}-\frac{8}{10}=1 \frac{7}{10}=1.7 \\
3 \frac{1}{2}-1 \frac{7}{10}=2 \frac{1}{2}-\frac{7}{10}=2 \frac{5}{10}-\frac{7}{10}=1 \frac{15}{10}-\frac{7}{10}=1 \frac{8}{10}=1 \frac{4}{5} \\
1 \frac{10}{10} \quad \text { He heads to lose } \\
1 \frac{8}{10} \mathrm{~kg}
\end{gathered}
$$

3. A construction company builds a new rail line from Town A to Town B. They complete $1 \frac{1}{4}$ miles in their first week of work and $1 \frac{2}{3}$ miles in the second week. If they still have $25 \frac{3}{4}$ left to build, what is the distance from Town A to Town B?


It is $28 \frac{2}{3}$ miles from Town $A$ to Town $B$.

COMMON CORE

Lesson 15:

Date:

Solve multi-step word problems; assess reasonableness of solutions using benchmark numbers. 8/7/13 engage ${ }^{\text {ny }}$
4. A catering company needs 8.75 lb of shrimp for a small party. They buy $3 \frac{2}{3} \mathrm{lb}$ of jumbo shrimp, $2 \frac{5}{8} \mathrm{lb}$ of medium-sized shrimp, and some mini-shrimp. How many pounds of mini-shrimp do they buy?


$$
\begin{aligned}
& 3 \frac{2}{3}+2 \frac{5}{8}=5 \frac{16}{24}+\frac{15}{24}=5 \frac{31}{24}=5+1 \frac{7}{24}=6 \frac{7}{24} \\
& 8 \frac{3}{4}-6 \frac{7}{24}=2 \frac{3}{4}-\frac{7}{24} \quad \text { They buy } 2 \frac{11}{24} \\
&=2+\left(\frac{3}{4} \times \frac{6}{6}\right)-\frac{7}{24} \quad \text { of mini-shrim } \\
&=2+\frac{18}{24}-\frac{7}{24} \\
&=2 \frac{11}{24}
\end{aligned}
$$

5. Mark breaks up a 9-hour drive into 3 segments. He drives $2 \frac{1}{2}$ hours before stopping for lunch. After driving some more, he stops for gas. If the second segment of his drive was $1 \frac{2}{3}$ hours longer than the first segment, how long did he drive after stopping for gas?


Start

$$
\begin{gathered}
2 \frac{1}{2}+2 \frac{1}{2}+1 \frac{2}{3} \\
5+1 \frac{2}{3} \\
6 \frac{2}{3}
\end{gathered}
$$

$$
\begin{gathered}
9-6 \frac{2}{3}=3-\frac{2}{3}=2 \frac{1}{3} \\
2 \frac{3}{3}
\end{gathered}
$$

Mark drove for $2 \frac{1}{3}$ hours after stopping for gas.

Lesson 15: using benchmark numbers. 8/7/13

Name $\qquad$ Date $\qquad$

1. Draw the following ribbons.
a) 1 road. The piece shown below is only $3 / 7$ of the whole. Complete the drawing to show the whole road.

b) 1 road. The piece shown below is $1 / 6$ of the whole. Complete the drawing to show the whole road.

c) 3 roads. $B$ is three times longer than $A$. C is twice as long as B. Draw the roads. What fraction of the total length of the roads is the length of $A$ ? If Road $B$ is 7 miles longer than Road $A$., what is the length of Road C?

## See correction on next page.

d) Write your own ribbon or road problem with 2 or 3 lengths.
Answers will vary.
$A \longmapsto$

$C \leadsto \sim \longrightarrow$
$B$ is $\frac{2}{6}$ or $\frac{1}{3}$ of
the total length.


Road $A$ is $\frac{1}{10}$ of the total.

